

DPP No. 48

Max. Time : 40 min.

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Topics : Vector, Application of Derivatives

Type of Questions		M.M., Min.
Subjective Questions (no negative marking) Q.1 to Q.8	(4 marks, 5 min.)	[32, 40]

- **1.** A segment of a line PQ with its extremities on AB and AC bisects a triangle ABC with sides a, b, c into two equal areas. Find the shortest length of the segment PQ.
- 2. Let f, g : [a, b] \rightarrow R be two continuous function, differentiable on (a, b). Assume in addition that g and

g' are no where zero on (a, b) and $\frac{f(a)}{g(a)} = \frac{f(b)}{g(b)}$. Prove that there exists $c \in (a, b)$ such that $\frac{f(c)}{g(c)} = \frac{f'(c)}{g'(c)}$

3. Let a, b, c, d, e, $f \in R$ such that ad + be + cf = $\sqrt{(a^2 + b^2 + c^2)(d^2 + e^2 + f^2)}$

Use vector to prove that $\frac{a+b+c}{\sqrt{a^2+b^2+c^2}} = \frac{d+e+f}{\sqrt{d^2+e^2+f^2}}$

- 4. Show that $f(x) = \left(1 + \frac{1}{x}\right)^x$ is always an increasing function for all x in its domain.
- 5. With usual notation in $\triangle ABC$ if 2b = 3a and $\tan^2 A = \frac{3}{5}$, prove that there are two values of third side, one of which is double the other.
- 6. Prove that the locus of the centre of a circle, which intercepts a chord of given length '2 a' on the axis of x and passes through a given point on the axis of y, distance b from the origin, is curve, $x^2 \pm 2yb + b^2 = a^2$.
- 7. Find the sum $\tan \theta + \frac{1}{2} \tan \frac{\theta}{2} + \frac{1}{2^2} \tan \frac{\theta}{2^2} + \frac{1}{2^3} \tan \frac{\theta}{2^3} + \dots \infty$ and hence the sum of the series

$$\frac{1}{2^2}\tan\frac{\pi}{2^2} + \frac{1}{2^3}\tan\frac{\pi}{2^3} + \frac{1}{2^4}\tan\frac{\pi}{2^4} + \dots \dots \infty$$

8. The two adjacent sides of a paralelogram are represented by the lines x - y + 1 = 0 and 4x-3y-2 = 0. If one of the diagonals of the parallelogram is along the line $y = \frac{3x}{2}$, then find the equation of the other diagonal without finding the vertices of the parallelogram.

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Answers Key

1.
$$\sqrt{\frac{(c+a-b)(a+b-c)}{2}}$$
 7. $\frac{1}{\theta} - 2\cot 2\theta$, $\frac{1}{\pi}$

8.
$$5x - 4y - 1 = 0$$

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